

EXERCISES OF WEEK THREE

Exercise 1. Suppose that there are two sentences P and Q such that

$$P \Leftrightarrow (P \Rightarrow Q).$$

Show that Q is true.

Exercise 2. Translate into the formal language the following sentence

“For every y there exists a unique x such that $f(x) = y$ ”

Exercise 3. In the following table

\in	A	B	C	D
A	0	1	0	1
B	1	0	0	1
C	0	1	0	0
D	0	0	0	0

Find the elements and the proper classes. State whether the following classes exist. In the affirmative case, find the classes they correspond to (for example, the empty class exists and $\emptyset = C$).

1. the complement class A'
2. $A \cap B$
3. $B \cup C$
4. the universal class \mathcal{U} .

Is the Class Construction Axiom satisfied?